

Natural Numbers : Set of counting numbers is called natural numbers. It is denoted by N. where,

$$N = \{1, 2, 3, \dots, \infty\}$$

Even Numbers : The set of all natural numbers which are divisible by 2 are called even numbers. It is denoted by E.

$$\text{Where, } E = \{2, 4, 6, 8, 10, \dots, \infty\}$$

Odd Numbers : The set of all natural numbers which are not divisible by 2 are called odd numbers. In other words, the natural numbers which are not even numbers, are odd numbers. i.e.,

$$O = \{1, 3, 5, 7, \dots, \infty\}$$

Whole Numbers : When zero is included in the set of natural numbers, then it forms set of whole numbers. It is denoted by W. where,

$$W = \{0, 1, 2, 3, \dots, \infty\}$$

Integers : When in the set of whole numbers, natural numbers with negative sign are included, then it becomes set of integers. It is denoted by I or Z.

$$I : [-\infty, \dots, -4, -3, -2, -1, 0, 1, 2, 3, 4, \dots, \infty]$$

Integers can further be classified into negative or positive Integers. Negative Integers are denoted by Z^- and positive Integers are denoted by Z^+ .

$$Z^- = \{-\infty, \dots, -3, -2, -1\} \text{ and}$$

$$Z^+ = \{1, 2, 3, \dots, \infty\}$$

Further 0 is neither negative nor positive integer.

Prime Numbers: The natural numbers which have no factors other than 1 and itself are called prime numbers.

Note that, (i) In other words they can be divided only by themselves or 1 only. As, 2, 3, 5, 7, 11 etc.

(ii) All prime numbers other than 2 are odd numbers but all odd numbers are not prime numbers.

2 is the only one even Prime number.

Co-Prime Numbers : Two numbers which have no common factor except 1, are called Co-Prime numbers. Such as, 9 and 16, 4 and 17, 80 and 81 etc.

It is not necessary that two co-prime numbers are prime always. They may or may not be prime numbers.

Divisible numbers/composite numbers : The whole numbers which are divisible by numbers other than itself and 1 are called divisible numbers or we can say the numbers which are not prime numbers are composite or divisible numbers. As, 4, 6, 9, 15,

Note : 1 is neither Prime number nor composite number. Composite numbers may be even or odd.

Rational Numbers : The numbers which can be expressed in the form of $\frac{p}{q}$ where p and q are integers and coprime and $q \neq 0$ are called rational numbers. It is denoted by \mathbb{Q} . These may be positive, or negative.

e.g. $\frac{4}{5}, \frac{5}{1}, -\frac{1}{2}$ etc are rational numbers.

Irrational Numbers : The numbers which are not rational numbers, are called irrational numbers. Such as

$$\sqrt{2} = 1.414213562.....$$

$$\pi = 3.141592653$$

Real Numbers: Set of all rational numbers as well as irrational numbers is called Real numbers. The square of all of them is positive.

Cyclic Numbers : Cyclic numbers are those numbers of n digits which when multiplied by any other number upto n gives same digits in a different order. They are in the same line. As 142857

$$2 \times 142857 = 285714 : 3 \times 142857 = 428571$$

$$4 \times 142857 = 571428 : 5 \times 142857 = 714285$$

Perfect Numbers : If the sum of all divisors of a number N (except N) is equal to the number N itself then the number is called perfect number. Such as, 6, 28, 496. 8128 etc.

The factor of 6 are 1, 2 and 3

$$\text{Since, } 6 : 1 + 2 + 3 = 6$$

$$28 : 1 + 2 + 4 + 7 + 14 = 28$$

$$496 : 1 + 2 + 4 + 8 + 16 + 31 + 62 + 124 + 248 = 496$$

$$8128 : 1 + 2 + 4 + 8 + 16 + 32 + 64 + 127 + 254 + 508 + 1016 + 2032 + 4064 = 8128. \text{ etc.}$$

Note : In a perfect number, the sum of inverse of all of its factors including itself is 2 always.

e.g. Factors of 28 are 1,2,4,7,14 are

$$= \frac{1}{1} + \frac{1}{2} + \frac{1}{4} + \frac{1}{7} + \frac{1}{14} + \frac{1}{28} = \frac{56}{28} = 2$$

Complex Numbers : $Z = a + ib$ is called complex number, where a and b are real numbers, $b \neq 0$ and $i = \sqrt{-1}$.

Such as, $\sqrt{-2}$, $\sqrt{-3}$ etc.

So, $a + ib$ or $4 + 5i$ are complex numbers.